A Compact Hydrogen Maser with Exceptional Long-Term Stability

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Abstract—A compact passive hydrogen maser with many unique features, including a significant reduction in size over previous hydrogen masers, is described. It uses the passive mode of operation, thereby permitting use of a small microwave $\text{TE}_{011}$ cavity which is dielectrically loaded by a low-loss alumina ($\text{Al}_2\text{O}_3$). The cavity is 14.6 cm outside diameter and 13.7 cm high, and weighs only 4.4 kg. The unloaded-cavity $Q$ factor is about 6000. With a conventional source, hexapole state selector, and four magnetic shields, the volume of the entire hydrogen maser resonator package is only about 20 l.

The FEP-coated quartz bulb which is common in other masers has been replaced by a similar coating on the inside wall of the cavity. This has yielded a simpler design and more rugged hydrogen maser package.

The cavity and attached endcaps compose the vacuum envelope, thus allowing use of a single vacuum system. The dimensional stability of the ceramic cavity under barometric changes is sufficiently within the range of the electronic cavity servo that a second vacuum system is not needed. For temperature control, a single oven is located in the magnetic shield nest.

The most recent stability data compiled from four compact hydrogen masers built at NBS is presented. Comparisons are made against the cesium standard NBS-4 and a time scale comprised of nine commercial cesium standards (denoted as 8s). The drift of the longest running measured maser ($H_4$) is undiscernible when compared against the time scale (UTC) composed of NBS-4 with the 8s time scale for two 69-day measurement durations.

INTRODUCTION

HYDROGEN MASER DEVELOPMENT in recent years has been directed toward a reduction in size without substantial compromise in frequency stability. Traditionally, the hydrogen maser has been an oscillator at approximately 1.42 GHz in the so-called "active" mode. However, a non-self-oscillating (or passive) configuration has been shown to reduce the long-term (greater than 10 days) drift and random-walk instabilities associated with active masers. The requirement for a high-$Q$ RF cavity surrounding the interrogated volume of H-atoms is relaxed. This makes possible new hydrogen maser designs, one of which is outlined in this paper.

At NBS, the concept of the passive rather than active maser was developed in order to obtain better long-term stability than that observed using active maser designs [1]-[3]. A quartz oscillator is locked to the hyperfine resonance using a design similar to optical pumping and atomic-molecular beam devices. Two important requirements of conventional self-oscillating masers have been relaxed: 1) a relatively high cavity $Q$ (needed for oscillation), and 2) excellent cavity frequency stability as a function of temperature, pressure, varactor voltage, and time. Item 2) is possible because in the passive mode of operation one has the ability to lock the frequency of the cavity to the H resonance. Passive electronics have been successfully deployed on a conventional full-size maser [1], [2]. The development of these new electronics makes possible a reevaluation of the design used in the maser (the so-called "physics package").

The maser works on the magnetic dipole transition of the ground state of free hydrogen atoms contained in a storage volume. Fig. 1 shows the $F = 0$ and $F = 1$ ground electronic states as a function of applied magnetic field. This hyperfine transition in hydrogen has a frequency of approximately $1420405751$ Hz. RF interrogation of the hydrogen atoms at this frequency takes place within a teflon-coated storage
In the passive mode, the hydrogen maser is not oscillating. The NBS maser electronics use two servo systems involving the cavity \( f_1 = 12 \text{ kHz} \) and the narrow H-line \( f_2 = 12 \text{ kHz} \). This wall-coating typically permits the hydrogen atoms to bounce \( 2 \times 10^4 \) times within this volume before losing their phase relative to the RF magnetic field.

In order to achieve high-filling factors, the average value of the instantaneous RF magnetic field needs to be in a certain direction over the entire hydrogen storage volume. One can develop cavity designs which yield small size and relatively high filling factor over a given volume [3]-[6]. The cavity design used here is a right circular cylinder of low-loss ceramic with a bore down the central axis and a silver coating on the outside. The ends are capped with \( \text{A}_2\text{O}_3 \) plates. The closed central bore is the hydrogen-storage volume. Along with a good filling factor, this geometry has the benefit of a high level of symmetry to better than 0.1 percent about all axes of the RF magnetic field in the storage volume. The \( \text{TE}_{011} \) mode is used. Therefore, in this new design, the microwave cavity forms the vacuum envelope and storage volume. With the loss given by currently available dielectric materials, this is only made possible because of the passive electronic scheme in which the maser is not oscillating.

Fig. 2 shows a block diagram of the passive maser scheme. A thorough explanation of the operation of the servo system is described in [1]-[3]. The interrogation (exciter) signal at 1420 MHz which enters the cavity is phase-modulated at two frequencies, \( f_1 \) and \( f_2 \). Frequency \( f_1 \) is a high-frequency (12-kHz) phase-modulation component used to probe the hydrogen cavity. Modulation component \( f_2 \) is used to probe the hydrogen resonance at 12-Hz modulation frequency. The two synchronously detected correction signals have different feedback time constants such that in the short term, the probe oscillator frequency is locked to the narrow hydrogen resonance. In the longer term, the cavity is tuned so that it is centered symmetrically about the probe frequency.

Full-size hydrogen masers typically also use a conventional \( \text{TE}_{011} \) mode microwave cavity with a diameter of about 21 cm and length of about 50 cm. The lumped constant equivalent circuit for such a cavity consists of an inductance \( L \) in series with a capacitance \( C \) in series with a resistance \( R \), as shown in Fig. 3. The insertion of a low-loss dielectric such as alumina (ceramic) affects the propagation constant, thus increasing \( C \) and decreasing the frequency of the cavity. The overall dimension of the cavity can then be reduced to compensate for the effect of the dielectric. RF symmetry, dielectric constant, overall dimension, and the hydrogen filling factor are all considered in order to achieve an optimum geometry. The net effect on the frequency of the \( \text{TE}_{011} \) mode must always be taken into account. Recall that the dielectric loading of the cavity affects the electric field. The RF magnetic \( H \) field (which excites the atoms) is uniquely determined relative to the orientation of the electric fields within the cavity by Maxwell’s equations. It is possible to choose a cavity inside diameter so that the spatial average of the axial component of the oscillating \( H \) field does not reverse phase within this open storage volume. Consequently, the inside bore can substitute for the storage bulb used in a conventional maser with little compromise in the filling factor (see Fig. 4). The filling factor is 0.5.1 A picture of the completed small maser cavity and shield assembly is shown in Fig. 4.

**Cavity Coating Technique**

The conventional hydrogen maser uses a quartz storage bulb with a teflon coating. The characteristics of hydrogen wall relaxation depend on the technique of coating application and the type and purity of teflon [7]. In the small passive maser, no quartz bulb is used and the coating is applied directly to the

\[ \eta = \frac{\langle B_r \rangle^2_{\text{storage}}}{\langle B \rangle^2_{\text{cavity}}} \]

where \( \langle B_r \rangle^2_{\text{storage}} \) is the mean value of the axial component of the amplitude of the magnetic field, averaged over the storage volume.

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1 In the hydrogen maser, the filling factor is defined as \( \eta = \frac{\langle B_r \rangle^2_{\text{storage}}}{\langle B \rangle^2_{\text{cavity}}} \).
inside wall of the ceramic dielectric. This is possible because the phase of the axial component of the RF magnetic field does not reverse in the hydrogen storage volume, but rather reverses inside the dielectric. The coating serves two purposes. The first is to provide a surface which minimally perturbs the phase of the hydrogen atoms; the second is to vacuum seal and bond the endcaps to the main cylinder.

The coating is made using Dupont FEP 120 emulsion. These resins in solution normally contain 50 percent water and about 8 percent triton X-100 stabilizer. The stabilizer tends to 1) keep the solid resin uniformly dispersed, and 2) lower the surface tension by acting as a wetting agent. A new liquid emulsion is then prepared by mixing 38 percent of the above solution to 52 percent H2O to 10 percent triton X-100 by volume. This new solution yields a thinner coat, slower initial drying phase, and better wetting of the ceramic surface than the original solution.

The liquid coating is applied to the ceramic endcaps with a polypropylene squeeze bottle. The surface is uniformly wetted and allowed to dry under a heat lamp for about 15 min. The endcap is placed in a kiln with a heat rise of about +6 K/min. Pure oxygen is flowed through the kiln during the heating cycles. FEP 120 is fused by melting at a temperature of 360°C. The rate of heating as one approaches 360°C is important because the high thermal mass of the ceramic causes the ceramic to lag the temperature of the kiln. Thus fusing of the coating tends to first take place at the outside surface of the coating, trapping stabilizers and other impurities within it. In order to avoid this, the rate of temperature increase should be reduced to approximately 1 K/min near 360°C.

Three layers of teflon are applied to the ceramic. This lowers the probability that microscopic cracks will increase the effective surface area and that ceramic may be exposed at the bottom of such cracks. Subsequent coats are applied by using the previous mix and allowing the solution to dry to a very thin overlayer. On the first wetting of the second and third coat, milky lumps may tend to form but this is of no consequence. After an initial dry, the solution is reapplied, wetting is more pronounced, and the lumps dissolve. The surface then dries as before in a uniform thin film, and the same kiln temperature cycle is used. After the first coat the surface has a matte finish. By the third coat the surface is glazed and clear.

The application of the teflon mix on the cylinder wall is the same as the application on the endcaps. It is useful to mount the cylinder in a lathe so that it can be rotated slowly while the liquid solution rolls on the inside wall. The wall is first uniformly wetted, then removed from the lathe and allowed to stand so that the liquid can drip to one end and the solution allowed to dry. Glass endcaps fitted with tubes which go out of the kiln are placed on the top and bottom of the cylinder during the oven cycle so that oxygen can be flowed through the inside bore of the cylinder. Here the oxygen serves two purposes: 1) to oxidize the stabilizer, and 2) to keep the outside surface of the coating cool relative to the temperature of the heating ceramic cylinder. This is done to insure that fusing first begins at the coating—ceramic boundary. A thermocouple is mounted in one of the RF slots on the cavity sidewall to monitor the temperature profile. Three layers are applied to the inside wall of the cylinder. Layers can be removed by increasing the oven temperature to about 650°C.

The same teflon used in the coating is also used as a glue to bond the ceramic cylinder. The bonding process involves wetting each endcap with its third (last) coat and fusing the coat while the endcap is attached to the cylinder. A 3-kg weight is placed on the endcap with the cylinder and endcap in an upright position. This presses cylinder and endcap together as the oven heats through the melting point and fusing temperature of the coating. The resultant teflon-loaded gap between endcap and cylinder is less than 25 μm (1 mil) thick, and the vacuum seal allows pressures of below 10^-9 torr in the cylinder.

The hydrogen resonance linewidth is 1 Hz, thus yielding \( Q = 1.4 \times 10^9 \). The storage volume is approximately 1 l. The value of the fractional frequency wall shift has not been measured and is not considered consequential to the objectives of high reproducibility of frequency and low drift. The fractional wall frequency shift is estimated to be of the order of \( 1 \times 10^{-11} \) based on the work of others [7].

**Frequency Stability Data**

In all, four hydrogen masers (H1 through H4) of the type described have been built at NBS. Frequency stability measurements of each were made against NBS-4 (a cesium primary standard) wherever possible and against each other in the case of H3 and H4. Some measurements have been reported [8] and are summarized here in addition to new long-term data on H3 and H4. H1 and H2 were not available simultaneously with H3 and H4 nor with each other since they were transported to other facilities soon after their construction. However, data were taken for 30-day periods between H1 and H2, each against NBS-4. Other standards used in comparisons were nine commercial cesium clocks in a single independent time scale denoted as 8s.
Identical designs were used for the four passive hydrogen masers. All had approximately the same hydrogen linewidths (between 1 and 2 Hz) and the same $S/N$ ratios.

Short-term stability measurements (from 1 to 10 000 s) on the hydrogen masers consistently produced the straight solid line shown on the stability plot of Fig. 5. This is the white-frequency behavior of the masers at $1.7 \times 10^{-12} \tau^{-1/2}$ and is the stability referred to each individual hydrogen maser. NBS-4 had the same (individual) stability of about $1.7 \times 10^{-12} \tau^{-1/2}$.

Long-term data were compiled based on approximately 30-day uninterrupted comparisons between each maser, NBS-4, and 8s. These three sources were treated as independent clocks. By simultaneously comparing three independent clocks, it is possible to deduce the stability of each individual clock. The points shown in Fig. 5, which extend beyond averaging times of 10 000 s, represent the individual performance of H3 and H4 in a three-way intercomparison. The relation for determining the stability of an individual clock in a three-way comparison is [9]

$$\sigma_i^2 = \frac{1}{2} [\sigma_i^2 + \sigma_k^2 - \sigma_j^2].$$  \hspace{1cm} (1)

The slight rise in $\sigma_i$ at averaging times of about one-half day and one day are most likely attributable to environmental effects (diurnal variations). Day-to-day temperature and pressure changes appear to enter at about the $1 \times 10^{-14}$ level. Although there is some degradation of stability for times around one day, the longer term stability is improving as shown by the last $\sigma_i$ point at an averaging time of eight days (4 data samples). The eight-day value of $\sigma_i$ is $8.1 \times 10^{-15}$ ($\pm 5.6 \times 10^{-15}$).

Figs. 6 and 7 show the frequency fluctuations as a function of time for H3. Fig. 6 shows a comparison between H3 and NBS-4, and Fig. 7 is the comparison between H3 and 8s. A more graphic comparative measure is the residual time fluctuations indicated in Figs. 8 and 9. Over a 32-day data run, Fig. 8 shows the time residual (taken from day-to-day epoch data) between H3 versus NBS-4. The time residuals are the integrated fractional frequency fluctuations. Fig. 9 shows the same plot of time residuals between H3 and 8s. For these data, the...
fluctuations are noticeably smoother in the comparison to the UTC ensemble of nine cesium clocks. The end points for these runs of data are deliberately set to return to zero time difference, thus removing an average frequency offset. In this 32-day data set, there appears to be correlated frequency changes of parts in $10^{-15}$ with period of the order of seven days. This possible effect is under further study.

Environmental temperature and barometric pressure measurements were made coincident with frequency in order to determine the level of sensitivity to these environmental effects. Interestingly, there is no perceivable barometric pressure effect to the level limited by the length of the data set. The barometric pressure changed by 7 percent (maximum) during this 32-day comparison. Other parameters were adjusted and their effects on the maser frequency are summarized in Table I.

### TABLE I

<table>
<thead>
<tr>
<th>EFFECT</th>
<th>OFFSET</th>
<th>INSTABILITY</th>
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<tbody>
<tr>
<td>1. Resonator Temperature</td>
<td>$3 \times 10^{-14}$K</td>
<td>$2 \times 10^{-15}$K</td>
</tr>
<tr>
<td>Sensitivity</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2. Spin Exchange</td>
<td>$2 \times 10^{-13}$</td>
<td>$2 \times 10^{-15}$</td>
</tr>
<tr>
<td>3. Magnetic Field</td>
<td>$1 \times 10^{-13}$</td>
<td>$10^{-15}$</td>
</tr>
<tr>
<td></td>
<td>($\pm 0.36$)</td>
<td></td>
</tr>
<tr>
<td>4. Power Dependence(microwave)</td>
<td>$10^{-13}$/dB</td>
<td>$10^{-15}$</td>
</tr>
<tr>
<td>5. Phase Modulator Drive</td>
<td>$10^{-13}$/dB</td>
<td>$10^{-15}$</td>
</tr>
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**Frequency Stability:** $<1.7 \times 10^{-12}/\text{hr}$, 1s to 10 s

**Drift vs. UTC(NBS):** $<1 \times 10^{-15}$/day (measurement limited)

H3. In these data, a linear drift term of $4 \times 10^{-15}$/day was observed and removed from the data, so the plot is the residual fractional frequency fluctuations. After degaussing, however, another measurement of 17 days was made which exhibited a drift versus UTC(X) of $7 \times 10^{-16}$/day $\pm 2 \times 10^{-15}$/day for H3 (UTC(X) is 8s with NBS included).

Fig. 10 shows the daily frequency fluctuations between H4 and 8s. The total number of days reported is about 200 with an interruption for magnetic shield degaussing. This was done because of a large magnet which was moved in the vicinity of H4, and as one sees from Fig. 10, there was an accompanying frequency change after degaussing.

It should be noted that except for one interruption to degauss the magnetic shields, H4 operated continuously for eight months at NBS, Boulder. Also H4 has not been adjusted or touched during this period.

The data presented in Fig. 10 are raw data; no drift has been removed and the measurement bandwidth is over 100 Hz. A linear drift has been fitted to two segments of the data. The first 69 days yield drift of $-1.82 \times 10^{-16}$/day. The second 69 days yield $+2.20 \times 10^{-16}$/day. These results are remarkable
for a hydrogen maser, and we conclude that the net drift is still below our ability to measure. In a comparison against UTC(NBS) the passive hydrogen maser showed no discernible drift over several weeks. The uncertainty in this level is about $2 \times 10^{-15}$/day over several weeks limited by the day-to-day fluctuations of UTC(NBS). If one assumes the drift is half the uncertainty, one can reasonably assume the drift to be no worse than $1 \times 10^{-15}$/day.

Random walk best characterizes the very long-term fractional frequency instabilities. Environmental changes of temperature and pressure appear to affect the maser stability at the $1 \times 10^{-14}$ level.

**CONCLUSION**

In this paper, frequency stability measurements on four passive hydrogen masers versus NBS-4 and UTC(NBS) have been presented. Frequency stability level is $1.7 \times 10^{-12} \tau^{-1/2}$ from 1 to $10^5$ s. No drift above $1 \times 10^{-15}$/day has been detected; this value is limited by measurement uncertainty of $2 \times 10^{-15}$/day. Some environmental sensitivity (pressure and temperature) affects frequency stability at about the $1 \times 10^{-14}$ level and the long-term (above $2 \times 10^5$ s) noise behavior is characterized as random walk. The long-term stability measurements presented here indicate great potential for the passive maser design as a clock and we are continuing to take measurements of H4 versus NBS-4 and UTC(NBS).

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**REFERENCES**


