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## Light shift suppression in a CPT magnetometer using linear polarization and double frequency interrogation

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**We demonstrate a suppression of the light shift in a Coherent-Population-Trapping (CPT) atomic magnetometer by using linearly polarized light and a differential measurement between magnetic resonances. The radio frequency that creates the optical sidebands for CPT quickly switches between two magnetic sensitive transitions, and the magnetic field is extrapolated from the difference of the center frequencies of the magnetic resonances. Light shifts and common drifts like collisional shifts can be suppressed through careful choice of measured resonances, and we show the light shift reduction by more than a factor of 20 compared to excitation with circularly-polarized light. Various limitations of the method are discussed.** © 2025 Optica Publishing Group. All rights, including for text and data mining (TDM), Artificial Intelligence (AI) training, and similar technologies, are reserved.

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Sensitive atomic magnetometers are useful in many areas of research, ranging from biomedical imaging [1,2] and material characterization [3,4] to tests of fundamental symmetries [5,6]. Due to their simplicity, high dynamic range, and low power consumption, atomic magnetometers based on Coherent Population Trapping (CPT) have previously been employed in space missions [7,8] where stability is critical [9–11].

The energy levels in atomic systems shift in the presence of optical fields. Such “light shifts” often significantly contribute to the long-term instability of a variety of atom-based instruments [12,13]. Such low-frequency noise of vapor-cell-based magnetometers has been characterized at sub-mHz level [14]. Understanding, and ultimately suppressing, this shift is therefore important in improving the long-term frequency stability of these types of instruments and enhancing their utility in application areas such as space science, geophysics, and magnetic anomaly detection.

For continuous wave (cw) clocks based on coherent population trapping, light shifts can be suppressed by appropriate choice of optical frequency [15,16]; sideband modulation

parameters [17–20]; or polarization of the probe light [21]. Unlike CPT clocks, which typically measure the center frequency of a single resonance of a magnetic-insensitive transition, magnetometers using linearly polarized light can interrogate multiple resonances simultaneously and provide simple extraction of vector field information, i.e., field orientation [22–24]. CPT magnetometers using linearly polarized light are also expected to suppress light shifts and other temperature-dependent drifts in vapor cells, such as the collision shift and quadratic Zeeman shift [22]. In this work, we demonstrate light shift suppression of a CPT magnetometer by using a linear-polarized laser beam and differential frequency detection between CPT resonances.

In the effective operator formalism [12,25], the light shift  $\delta E$  in atomic systems can be expressed in terms of the electric field  $\mathbf{E} = \varepsilon_0 e^{i(\mathbf{k}\cdot\mathbf{r} - \omega t)} \boldsymbol{\zeta} + c.c.$ , where  $\boldsymbol{\zeta}$  represents the complex polarization vector, and the polarizability operator  $\alpha^L$  (L: scalar, vector, and tensor) [25]:

$$\begin{aligned} \delta E &= \delta E_0 + h\delta\mathbf{AI} \cdot \mathbf{J} - \boldsymbol{\mu} \cdot \delta\mathbf{H} + \delta\varepsilon_2 \\ &= -\frac{1}{8} |\varepsilon_0|^2 \sum_L (\boldsymbol{\zeta}^* \cdot \alpha^L \cdot \boldsymbol{\zeta} + \boldsymbol{\zeta} \cdot \alpha^{L\dagger} \cdot \boldsymbol{\zeta}^*). \end{aligned} \quad (1)$$

Here,  $\delta E_0$  is a common shift of all sublevels that has no impact on the transition frequencies and  $h\delta\mathbf{AI} \cdot \mathbf{J}$  is the scalar light shift that shifts all Zeeman levels within a given hyperfine manifold equally. When the field polarization is not perfectly linear, the transition frequency has the Zeeman (vector) light shift contribution of  $\boldsymbol{\mu} \cdot \delta\mathbf{H}$ , where  $\delta\mathbf{H}$  is an effective magnetic field proportional to the light intensity. The final term  $\delta\varepsilon_2$  is the tensor light shift that significantly contributes to the total shift when the Doppler broadening of the excited-state is smaller than its hyperfine splitting [12].

In a CPT magnetometer, two light fields illuminate the atomic ensemble in a  $\Lambda$  configuration,  $\mathbf{E}_{1,2} = \varepsilon_{1,2} e^{i(\mathbf{k}_{1,2} \cdot \mathbf{r} - \omega_{1,2} t)} \boldsymbol{\zeta}_{1,2} + c.c.$  with their frequency difference approximately matching the ground-state hyperfine splitting  $\nu_{HF}$  (6.834 GHz). In the presence of a magnetic field  $B$ , the frequency of the transition

between two  $\Lambda$ -coupled Zeeman states  $|F_1, m_{F_1}\rangle$  and  $|F_2, m_{F_2}\rangle$  is given to first order in  $B$  by [26]:

$$\nu_R(n, \Delta m) = \frac{\delta \varepsilon_{n, \Delta m}}{h} \approx (g_J - g_I) \frac{\mu_B B}{8h} n + g_I \frac{\mu_B B}{h} \Delta m, \quad (2)$$

where  $g_J$  and  $g_I$  are the electronic and nuclear g-factors respectively,  $\mu_B$  is the Bohr magneton and where  $n = m_{F_1} + m_{F_2}$  and  $\Delta m = m_{F_2} - m_{F_1}$  are restricted by the two-photon selection rules. The resulting spectrum is a series of doublets with the coarse structure determined by the electronic Zeeman splitting (the first term to the right of the approximation sign in Eq. (2)) and each doublet split by the much smaller second term due to the nuclear magnetic moment. A measurement of the difference in frequency  $\Delta \nu^B$  between two resonances ( $n_1, \Delta m_1$ ) and ( $n_2, \Delta m_2$ ), can then precisely determine the magnitude of the magnetic field as:

$$\Delta \nu^B = [(g_J - g_I) \frac{\mu_B}{8h} (n_1 - n_2) + g_I \frac{\mu_B}{h} (\Delta m_1 - \Delta m_2)] B. \quad (3)$$

In the presence of the light, the two-photon resonance condition is further modified by the interaction of the optical fields with the atoms, and the measured frequency shift becomes:

$$\Delta \nu_{meas} = \Delta \nu^B + \Delta \nu^l(\omega_1, \omega_2). \quad (4)$$

The additional term produces a systematic error and limits the sensitivity with which the magnetic field strength can be determined in the presence of polarization, frequency, or amplitude noise on the optical field. For a particular  $n$ , the effective shift of the corresponding CPT transition  $\nu_n^l$  is given by the differential light shift of the two coupled levels  $m_{F_{1,2}}$ , and can be separated into its three contributions as in Eq. (1) [27]:

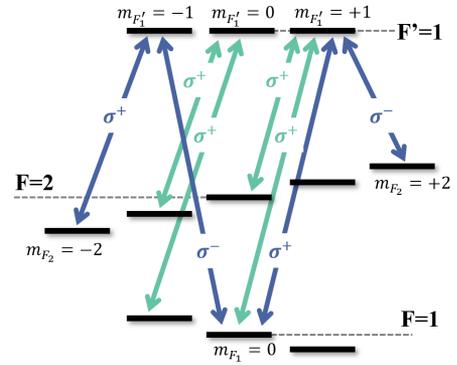
$$\nu_n^S = - \left( \frac{\varepsilon_2}{2} \right)^2 / h \{ [q\alpha_2^S(\omega_1) + \alpha_2^S(\omega_2)] - [q\alpha_1^S(\omega_1) + \alpha_1^S(\omega_2)] \}, \quad (5)$$

$$\nu_n^V = - \left( \frac{\varepsilon_2}{2} \right)^2 (\mathbf{k} \cdot \hat{\mathbf{B}}) \mathcal{A} / h \left\{ \frac{m_{F_2}}{4} [q\alpha_2^V(\omega_1) + \alpha_2^V(\omega_2)] - \frac{m_{F_1}}{2} [q\alpha_1^V(\omega_1) + \alpha_1^V(\omega_2)] \right\}, \quad (6)$$

$$\nu_n^T = - \left( \frac{\varepsilon_2}{2} \right)^2 (3|\boldsymbol{\zeta} \cdot \hat{\mathbf{B}}^2 - 1) / h \left\{ \frac{3m_{F_2}^2 - 6}{12} [q\alpha_2^T(\omega_1) + \alpha_2^T(\omega_2)] - \frac{3m_{F_1}^2 - 2}{2} [q\alpha_1^T(\omega_1) + \alpha_1^T(\omega_2)] \right\}, \quad (7)$$

where  $\hat{\mathbf{B}}$  is the unit vector along the quantization axis.  $\alpha_F^{S,V,T}(\omega)$  are the scalar, vector, and tensor polarizabilities of the ground state  $F$  induced by the optical field with frequency  $\omega$ . The field's amplitude  $\varepsilon_1^2$  is written as a fraction of  $\varepsilon_2^2$  ( $\varepsilon_1^2 = q\varepsilon_2^2$ ), where  $q$  is fixed for a given RF modulation index. The symbol  $\mathcal{A}$  represents its degree of circular polarization ( $\mathcal{A} = \pm 1$  for  $\sigma^\pm$ -polarized light and  $\mathcal{A} = 0$  for linearly-polarized light). Only the vector  $\nu_n^V$  and tensor  $\nu_n^T$  parts contribute to  $\Delta \nu^l$  in Eq. (4) when taking the differential shift between any two CPT transitions. The scalar component  $\nu_n^S$  is a common shift that doesn't depend on the specific  $m_F$  values and therefore vanishes when taking the difference of any pair of CPT resonance frequencies.

For a CPT magnetometer with circularly-polarized light and atoms with nuclear spin 3/2, only two resonances are present in the spectrum and correspond



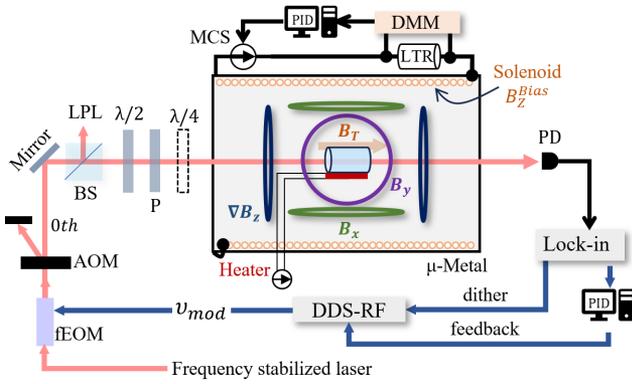
**Fig. 1.** Energy level diagram of the D1 line of  $^{87}\text{Rb}$ . The arrows represent the different  $\Lambda$ -schemes created with circularly (green) and linearly (blue) polarized light to excite the  $n = \pm 2$  transition.

to transitions  $|F = 1, m_{F_1} = 0\rangle \leftrightarrow |F = 2, m_{F_2} = 0\rangle$  and  $|F = 1, m_{F_1} = -1\rangle \leftrightarrow |F = 2, m_{F_2} = -1\rangle$ , represented by green arrows in Fig. 1. Both the vector and tensor components of the light shift contribute here since  $|\mathcal{A}| = 1$  and each transition has different magnitudes of  $m_{F_1}$  and  $m_{F_2}$ . When using linear polarization,  $\mathcal{A} = 0$  in Eq. (6) and the vector light shift is completely suppressed for all CPT transitions. The tensor shift can be further canceled by measuring the differential shift of two transitions with  $m_F$ 's of the same magnitude. Such a pair exists on the D1 line of  $^{87}\text{Rb}$ , and are given by  $|F = 1, m_{F_1} = 0\rangle \leftrightarrow |F = 2, m_{F_2} = -2\rangle$  (for  $n = -2, \Delta m = -2$ ) and  $|F = 1, m_{F_1} = 0\rangle \leftrightarrow |F = 2, m_{F_2} = +2\rangle$  (for  $n = +2, \Delta m = +2$ ) and are schematically represented by the blue arrows in Fig. 1.

In this work, we show experimentally that the vector and tensor light shifts can indeed be suppressed by a factor of more than 20 using CPT excitation with linearly polarized light.

We excite the CPT transitions at 795 nm in a heated glass-blown vapor cell with an inner volume of  $1 \text{ cm}^3$ , as shown in Fig. 2. A Ne buffer gas with 1.3 kPa of pressure is added to increase the coherence time of the atoms. The laser frequency is locked to the  $F = 2 - F' = 1$  transition in a reference cell with an offset lock technique to compensate for the buffer gas shift of the excited transitions. The bi-chromatic field for the CPT process is generated using a fiber-coupled electro-optical modulator (EOM). The two-photon resonance is satisfied using the carrier and 1st sideband at a modulation frequency of approximately  $\nu_{mod} = 6.8 \text{ GHz} + \nu_R(n, \Delta m) + \nu^l$ .

The laser power is stabilized using an acousto-optic modulator (AOM). The vapor cell is placed in a controlled magnetic field environment inside a multi-layer  $\mu$ -metal shield. The quantization axis in the  $\mathbf{z}$  direction is defined by a longitudinal magnetic field  $\mathbf{B}_T$ , produced by a solenoid, generating a longitudinal field  $\mathbf{B}_z^{Bias}$ , and two sets of perpendicular saddle coils, generating transverse fields  $\mathbf{B}_x$  and  $\mathbf{B}_y$ , with which the direction of the applied field can be fine-tuned to be along the wave-vector of the light,  $\mathbf{k}$ . An extra pair of coils in an anti-Helmholtz configuration generates a field gradient  $\nabla B_z$  with which magnetic gradients internal to the shield can be compensated. The solenoid current (MCS) is monitored and stabilized using a low-temperature-coefficient resistor (LTR-Fig. 2) and a digital multimeter (DMM-Keysight 3458A-Fig. 2). A polarizer before the cell suppresses the polarization components perpendicular to its optical axis by more than a factor of 40 dB. A photodetector (PD) after the cell measures the transmitted light.

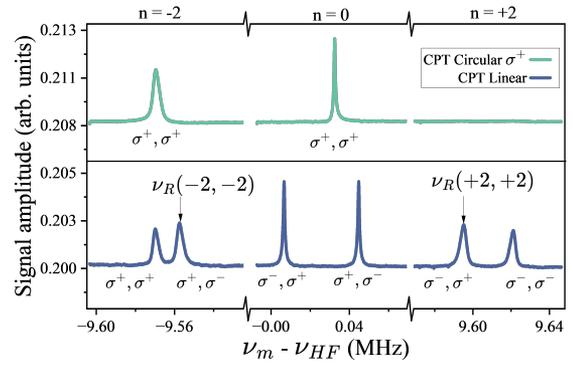


**Fig. 2.** Experimental setup. BS, beam splitter; DMM, digital multimeter; fEOM, fiber electro-optical modulator; LPL, laser power lock; LTR, low temperature coefficient resistor; MCS, main current source; P, polarizer; PD, photo-detector.

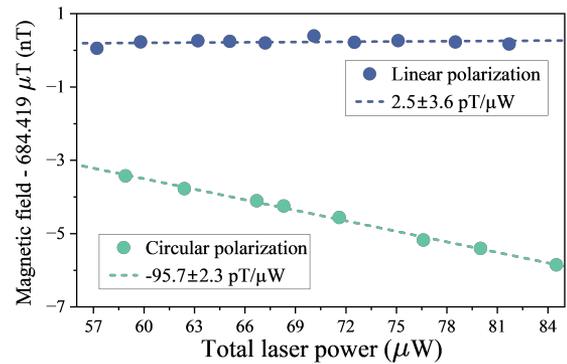
We determine the resonance frequency of the CPT transitions by slowly (230 Hz) dithering the frequency  $\nu_{mod}$  of the RF field and locking it to the zero-crossing of the dispersive error signal generated by a lock-in amplifier. A direct digital synthesis (DDS) is used to hop the modulation frequency  $\nu_{mod}$  between two CPT resonances at a rate of  $\approx 1$  s to further determine the differential frequency shift  $\Delta\nu_{meas}$  between the two transitions. The hopping rate does not represent the intrinsic bandwidth of the magnetometer or the proposed method being investigated here, which is instead fundamentally limited by the CPT linewidth ( $\approx 1$  kHz for the cell used here), with a modest reduction due to the dead time between hops. Frequency hopping helps to remove the influence of atomic collisions with the buffer gas, which cause a common drift in the CPT spectrum produced by changes in the cell temperature.

When the light propagation direction is perfectly aligned with the magnetic field, a linear polarization excites both  $\sigma^+$  and  $\sigma^-$  transitions. At high magnetic fields, a doublet forms at each  $n = \pm 2$  resonance, created by the  $\Delta m = 0$  (for  $\sigma_+/\sigma_-$ ) and  $\Delta m = 2$  (for  $\sigma_+/\sigma_-$ ) transitions in Fig. 1. As described above, the doublet in the CPT spectrum is a result of the nuclear magnetic moment [26]. At moderate magnetic fields, these resonances overlap and create ambiguity in the measurement of the resonance frequency. To resolve the  $n = \pm 2$  transitions, a strong magnetic field  $B^T$  of  $684 \mu\text{T}$  is applied, which splits the doublets by approximately 26 and 12 kHz, respectively. The field gradients at such a field strength do not significantly broaden the resonances, thereby maintaining reasonable resolution for the measurement of the resonance frequencies. A smaller field may be used if the resulting doublet splitting still exceeds the resonance linewidth, such as in the case of larger cells. Alternatively, in situations where the field orientation can be controlled, the  $\pi$ -polarization eliminates the doublet structure allowing the operation at any magnetic field strength.

The CPT spectrum produced by linearly polarized light at this field is shown by the blue trace in Fig. 3. There is an overall shift of all the resonances with respect to the hyperfine frequency of the unperturbed clock transition  $\nu_{HF}$  due to the presence of the buffer gas. The linewidth of the  $n = \pm 2$  peaks is broadened to 3.7 times that of the clock  $n = 0$  transitions (approximately 1 kHz) by the residual magnetic field gradient (roughly 200 nT/cm). The green trace in Fig. 3 is the CPT spectrum obtained using circularly polarized light. Here,



**Fig. 3.** CPT transitions excited by circular and linear polarizations.



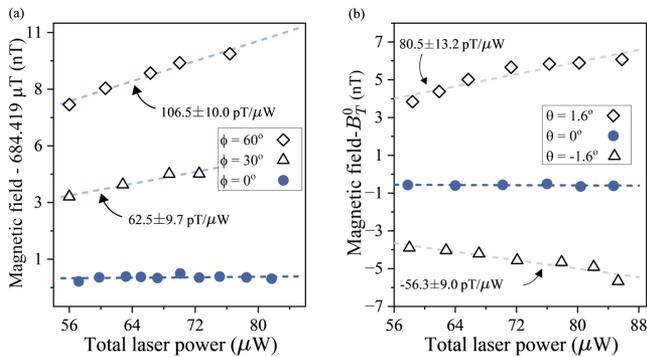
**Fig. 4.** Differential light shifts for circular (green) and linear polarization (blue).

the  $\Delta m = 2$  resonances are not excited, leaving only the singlet  $\Delta m = 0$  resonances.

For circularly polarized light, we measure a differential shift between the  $n = 0$  and  $n = -2$  transitions that varies with optical power. The corresponding value of the magnetic field is calculated from the measured frequency shift using the Breit-Rabi equation and the result is plotted in green in Fig. 4. The scalar light shift is canceled in the differential frequency measurement, so the vector and tensor components are the major contributions to the measured shift, with a slope of  $-95.7 \pm 2.3$  pT/ $\mu\text{W}$ . In the case of linear polarization, the differential shift is measured between the pair of the  $n = \pm 2$  transitions as  $\nu_R(\pm 2, \pm 2)$  in Fig. 3 and blue arrows in Fig. 1.

We observe no measurable change in extracted magnetic field over the entire range of laser powers, consistent with complete suppression of the vector light shift within the resolution of our measurements. A linear fit to the data returns a light shift coefficient of  $2.51 \pm 3.61$  pT/ $\mu\text{W}$ , consistent with zero. The vector light shift vanishes with linear polarization, and the scalar as well as tensor light shift also cancel when measuring the difference in transition frequency of  $n = \pm 2$ .

The light shift coefficient is reduced from  $95.7 \pm 2.3$  pT/ $\mu\text{W}$  with circular polarization to  $2.51 \pm 3.61$  pT/ $\mu\text{W}$  with linear polarization, resulting in a cancellation by more than a factor of 20, even at the highest laser powers. In addition, when we extrapolate the magnetic field to zero intensity in each polarization case, the resulting measured fields are equal within 2 nT, given by  $684.4212 \pm 0.0002 \mu\text{T}$  for the circular polarization and  $684.4191 \pm 0.0003 \mu\text{T}$  for the linear polarization.



**Fig. 5.** (a) Light shift dependence on the optical axis alignment. (b) Light shift dependence on the  $\mathbf{k}$  and  $\mathbf{B}_T$  alignment.

The suppression of the light shift observed here for linear polarization implies that fluctuations in laser power should have a substantially reduced effect on the magnetometer output, thereby improving the long-term magnetometer stability and potentially its accuracy also. However, there are several factors that could limit this enhancement of performance. At higher laser powers and weak fields, power broadening results in overlap and distortion of the resonances as the doublets merge into a single peak, which contaminates the measurement of their individual resonance center frequencies. In addition, polarization noise that changes the optical pumping and hence the population ratio of states would change the relative signal amplitude within the merged doublet and shift center frequency, thus contributing to corresponding field instability.

Stress-induced birefringence of optical components between the polarizer and the atoms, which adds a small degree of circular polarization to an otherwise linearly polarized beam, also shifts the resonance center frequency and affects the light-shift stability.

When rotating the linear polarization axis with the laser beam propagating along  $\mathbf{B}_T$ , we observed that the slope of the light shift changed with the angle  $\phi$  of linear polarization. This is due to a small birefringence of the input window of the vapor cell. The light shift coefficient varies by about 1.8 (pT/μW)/degree when the linear polarization is close to the optical axis of the cell window, as shown in Fig. 5(a).

The light shift coefficient also changes noticeably by about 43 (pT/μW)/degree if there is a misalignment of the laser beam with respect to the magnetic field, as shown in Fig. 5(b). Here we changed the angle  $\theta$  between  $\mathbf{k}$  and the bias field by changing the magnitude of the perpendicular field  $\mathbf{B}_x$ . The new bias field has a magnitude of  $B_T^0 = \sqrt{B_T^2 + B_x^2}$  with a relative angle  $\theta = \tan^{-1}(B_x/B_T)$  with respect to its original direction  $\mathbf{B}_T$ . The origin of this orientation dependence remains unclear, since the vector light shift should vanish for linearly polarized light; Eq. (6) holds for any field orientation. Moreover, the differential measurement should suppress the scalar and tensor light shifts in Eqs. (5) and (7) when the light couples to the same ground-state hyperfine level. We include this data for completeness, and the residual shift in the presence of transverse fields will be explored in future work.

The sensitivity of our magnetometer is limited by noise in the bias magnetic field, which we have measured using standard fast Fourier transform (FFT) measurements and estimated to approximately 200 pT/ $\sqrt{\text{Hz}}$  at 10 mHz. Nevertheless, our work demonstrates that the light shift of CPT magnetometers can be

suppressed by more than an order of magnitude with linear polarized light fields and differential measurement between  $n = \pm 2$  resonances with the same  $\Delta m$ ; a corresponding improvement in low-frequency noise is expected. Such a stable magnetometer is expected to benefit applications in space science and electrical metrology, where long-term magnetometer stability and accuracy are desired.

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**Data availability.** Data underlying the results presented in this work may be obtained upon request.

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