A STUDY OF POINT-CONTACT JOSEPHSON JUNCTIONS FOR USE IN FREQUENCY SYNTHESIS

Allan S. Risley
Frequency & Time Standards Section
National Bureau of Standards
Boulder, CO 80302

ABSTRACT

A carefully controlled microwave experiment using point-contact Josephson junctions (PCJJ) is reported. The experiment measures the IF power, $P_{\text{IF}}$, generated in low-order frequency multiplication and mixing. Also measured is the number of induced steps produced by the microwave source. Four characteristics possessed by PCJJ’s which gave the largest $P_{\text{IF}}$ are described. These criteria are compared to those which were obtained in studies previously reported. There is good agreement with three of these criteria and the discrepancy with the fourth is discussed in detail.

An operational procedure for fabricating a good PCJJ is described. The four most important potential high frequency limitations of a PCJJ are discussed with respect to the experimental results. This paper reports the use of a non-superconducting whisker plated with a superconductor.

INTRODUCTION

At the National Bureau of Standards we intend to phase-lock a far-infrared (FIR) laser to an X-band signal [1-3]. The aim is to be able to compare the frequency of a microwave source to that of a laser source, without losing cycle identification, at laser frequencies at least as high as 4.25 THz (70.5 μm). The large frequency multiplication orders, $N$, required indicate that the point-contact Josephson junction (PCJJ) is presently the best candidate for the multiplier and mixer. This paper discusses a microwave experiment aimed at improving the understanding and reliability of PCJJ’s.

While the PCJJ has performed $N = 401$ (starting at X-band) [4] and $N = 825$ (starting at 1 GHz) [5] the reliability is inadequate for the present application. The practical problem is to learn how to make PCJJ’s of sufficient quality and reliability. Junctions capable of giving a signal-to-noise ratio of at least 20 dB (in a 1 kHz bandwidth) for $N = 500$ is the goal.

The empirical results of NBS [6] and those of NPL [7] evolved four criteria which appear to characterize a good PCJJ for use at large $N$ and specifically, where the upper frequency source is in the FIR. They are:

1. The critical current, $I_0$, should be of the order of 250 μA. Critical currents lower than 50 μA and higher than 1 mA are outside the optimum range.
2. The product, $I_0 R$, (where $R$ is the asymptotic resistance of the junction) should be of the order of 1 mV or greater.
3. The undriven $I-V$ curve should show evidence of an "energy-gap" structure. (The dc component of the total current through the junction is $I$ and that component of the voltage across it is $V$.)
4. The junction should show at least the first step in the $I-V$ curve due to the laser drive, $V_{\text{laser}}$.

Presumably these empirical observations have an important relationship to the four major features that potentially limit the $N$ value and maximum value of $V_{\text{laser}}$. These limitations are:

- The spreading of the spectrum of the super-current as $N$ increases [8].
- High-frequency limitations of the Josephson effect due to the finite binding energy (i.e., the energy gap) of superconducting electron pairs [9].
- Localized heating (due to the driving sources) which lowers $I_0$ [10].
- The shunting of high-frequency currents due to the non-zero capacitance of the contact [11].

II. THE EXPERIMENT

In the experiment reported here, both simple mixing ($N = 1$), and third harmonic generation and mixing ($N = 3$) are studied. Two X-band sources are used in the first case, and an X-band and a K-band source are used in the second. The measured quantities are the intermediate frequency power, $P_{\text{IF}}$, and the voltage extent of the steps in the $I-V$ curve produced by the microwave sources [7, 12, 13].
Experience has shown - but not satisfactorily explained - the importance of several parameters to the generation of a useful level of \( P_{IF} \). These are: the maximum supercurrent, \( I_o \); the asymptotic resistance, \( R \); the product, \( I_o R \); and the dc component of the voltage across the junction, \( V \) [4, 14-17]. Figure 1 defines these quantities.

A block diagram of the experimental set-up is given in figure 2. A few comments need to be made about some of the components: When the microwave switch is in positions 2 or 3, the junction is irradiated with both microwave sources and the system is set up for measuring \( P_{IF} \). When the switch is in position 1, the junction is only irradiated by source \#1 and the system is set up for measuring steps in the I-V curve.

The break between the waveguide and coaxial tees, and the 1.4 GHz coaxial filter, provide isolation such that the PCJJ is the only dc path that the bias box sees. This allows a known bias to be put on the junction and permits observation of the I-V curve. In addition to this function, the coaxial filter provides impedance matching at \( f_{IF} \) (= 1.4 GHz) and rejection of the two microwave drives.

The Josephson junction mount fits directly into an ordinary storage dewar and is coaxial in structure. The whisker for the junction forms the extreme end of the center conductor, and the post forms a short at the end of the shield. The probe is inserted into the dewar with the junction open (i.e., the whisker not contacting the post) and the junction is closed only after the device comes to temperature. This allows the formation of contacts of sufficient sensitivity to be of interest.

### III. EXPERIMENTAL RESULTS

Table I displays the two variables, \( P_{IF} \) and voltage-extent of steps, versus the four parameters. Rather than list the total number of observable microwave steps, I have listed that value of \( V \) at which the last observable step occurs. [Steps whose full height was as small as about 5 \( \mu \)A were observable. With reduction of the noise fed to the junction it is possible to study steps as small as a few nanocentimeters [18]. In retrospect, it is unfortunate that it was not possible to resolve smaller steps because this might have permitted a more definitive interpretation of the data (see Section IV)]. The reason for this is that the self-oscillation frequency is directly proportional to \( V \) (\( v_o = 484 \text{ MHz/\mu V} \)) and the appearance of a step is evidence of a zero-beat between \( v_o \) and a harmonic of the drive signal. The original thought was that the extent of the steps in any given junction would be a measure of the high-frequency cut-off of that junction. This does not, however, seem to be the case.

There are several main features to be noted in this table:

1. If \( P_{IF} \) is greater than about 40 dB above the noise (in a 30 kHz bandwidth), steps are not observed. If \( P_{IF} \) is less than about 40 dB there are (usually) well defined steps.

2. Based on 21 contacts, \( P_{IF} \) greater than 50 dB above the noise correlates fairly well with \( I_o R > 0.8 \text{ mV} \).

3. Based on 21 contacts, the absence of steps correlates rather well with \( R > 2 \text{ ohms} \).

4. Based on 11 contacts, the voltage extent of the steps is not well correlated with \( I_o \).

Several other things are important to mention: At the time these data were taken, it was not possible to measure asymptotic resistance smaller than about 1 ohm. Thus, for many contacts, an accurate value of \( I_o R \) is not available and the corresponding \( I_o R \) element has been left blank.

An entry of N.M. in the \( P_{IF} \) column just means that \( P_{IF} \) was sufficiently low as not to be of interest, say, less than 35 dB.

If the initial or subsequent contacts of the whisker to the post are too violent, then the whisker will be blunted to the extent that a hysteretic I-V curve may result. An entry of Y in the hysteretic column means that this has happened. Further discussion of this subject is given at the end of this section.

The output, \( P_{IF} \), does not necessarily have a single maximum versus \( V \). In fact, for low levels of microwave drive, there will be very sharp peaks in \( P_{IF} \) versus \( V \) [8]. However, as the drive power is increased these several maxima broaden until finally there is but a single very broad maximum. [Actually, a maximum for positive \( V \) and one for negative.] Sometimes the maximum output that could be obtained occurred before these maxima coalesced. In any case, the last column lists that value of \( V \) corresponding to the set of \( P_{drive} \)
V values that maximized \( P_{IF} \). All the \( P_{IF} \) data of Table I (and the corresponding V's) were taken for \( N=3 \). For this case, \( P_{IF} \) is much less sensitive to \( P_{K-band} \) than it is to \( P_{X-band} \). To first-order, (for the \( N = 3 \) case) the optimum drive level (and this applies to both sources) is that which produces the maximum number of steps in the I-V curve. [It might be suggested that the smaller amount of \( P_{IF} \) that occurred with the low resistance junctions was just an impedance matching problem. This does not appear to be the case. A separate test indicates that the coaxial filter (fig. 2) can be adjusted to provide a good match to junctions ranging from 1 ohm to about 200 ohms. The filter was adjusted to maximize \( P_{IF} \) for each contact.]

The data of Table I were taken using six different whiskers. Three of the whiskers were made from solid niobium (Nb) wire of 0.005 cm (0.002 inches) diameter. One was made from solid Nb of 0.013 cm (0.005 inch) diameter. The other two were made from presharpened 0.005 cm (0.002 inch) diameter tungsten (W) wire which was subsequently plated with about 1 \( \mu \)m of Nb. To my knowledge, the present work represents the first use of plated PCJJ's for multiplication and mixing. The solid Nb whiskers were pointed by etching in pure hydrofluoric acid.

An examination of the table shows that for every case in which \( P_{IF} \) was greater than 40 dB above the noise, the whisker used was either the 0.013 cm (0.005 inch) diameter solid Nb or of the Nb-plated W type. The probable reason for this is the extreme difficulty in making a junction with a large \( I_o R \) product and with \( I_o \) of the order of 250 \( \mu \)A when using the 0.005 cm (0.002 inch) Nb whisker. The usual problem is that, as a person attempts to get an acceptably large \( I_o \), the tip bends over and presumably such a large contact area results that the contact resistance becomes quite small and, at the same time, the supercurrent becomes excessively large.

A person intuitively feels that the \( I_o, R \) and capacitance values of a given junction will depend upon whisker preparation (e.g., sharpness of point, state of oxidation) and upon the procedure of contacting the whisker to the post. The junctions that are available for study in a given experiment will then depend upon these fabrication conditions and their variability. As the discussion in items c and d of section IV imply, important things go on in dimensions that are of the order of the wavelength of visible light and smaller. If one understood the microscopic details of the contact he might be able to explain why some contacts work well and others don't. In the absence of this knowledge one can only hope for a procedure that has a high probability of producing high quality junctions. During the course of the present work such a procedure was developed and is described in the appendix.

IV. DISCUSSION

With section III as background, it is now appropriate to reexamine points 1-4 of section I.

The data of Table I correlate well with the idea that \( I_o \) needs to be of the order of 250 \( \mu \)A to produce good \( P_{IF} \). It might be suggested that the \( I_o \) criterion and the \( I_o R \) criterion are not independent, that setting \( I_o \) to about 250 \( \mu \)A automatically gives a large \( I_o R \) product (The theoretical maximum \( I_o R \) for Nb is \( \approx 2.4 \) mV). Table I seems to deny this because there are four contacts (\#s 16, 11, 20 and 7) that satisfy the \( I_o \) criterion but whose resistance is low. It appears, therefore, that an \( I_o R \) product of the order of 1 mV or greater is an independent and important criterion.

With respect to the energy-gap, four of the 21 contacts exhibit energy gap structure in their I-V curves. Figure 1 is, in fact, the I-V curve of contact 18. Each of these four contacts produced \( P_{IF} \) of 53 dB or greater. The largest other output was 51 dB produced by contact 15 and it exhibited a "pathological" I-V curve. It is important to note that the energy gap criterion correlates very well with the \( I_o \) and \( I_o R \) criteria discussed in the proceeding paragraph.

Regarding steps in the I-V curve, the most surprising result is the strong negative correlation between the presence of microwave steps in the I-V curve and the level of \( P_{IF} \). I do not have a quantitative explanation for this. There are, however, two qualitative things that can be said about factors that make steps difficult to see. First, noise will round the edges of the steps. The lower the frequency of the source which produces the steps, the closer spaced the steps will be. Close spacing in addition to noise rounding decreases the clarity of the steps. Second, for a given voltage spacing \( \Delta V \) between steps, the current spacing between their centers, \( \Delta I \), will decrease with increasing resistance, i.e., \( \Delta I = \Delta V/R \). If some mechanism prohibits the steps from being hysteretic, then their full height is limited to \( \Delta I \). Apparently such a mechanism exists because the only induced steps
of which I am aware] that show hysteresis are associated with a closely coupled cavity resonance [19] which is not the case in the present work. Zimmerman and Sullivan have proposed that the absence of hysteresis in induced steps is due to noise which causes the junction to make a transition from the higher to the lower of the two possible energy states [20].

In the present experiment, steps were produced with the K-band source as well as the X-band. This was done by setting the attenuator for source #1 (the X-band source common to both the N=1 and N=3 experiments) to maximum. The switch was then put in position 3 and the junction irradiated with the K-band source. Any contact for which X-band steps could be produced also produced K-band steps. A contact that would not show X-band steps did not show K-band steps. The qualitative arguments given above probably bear on the unobservability of the steps but a quantitative explanation is lacking.

An important practical problem when a laser is used as the high frequency source is the difficulty in focusing upon the junction. In the past- when failing, after some effort at trying to get the PCJJ to respond to the laser - the quality of the junction has come into question. I presently believe that, if the $I_0$, $I_R$, and energy gap criteria are all met, the junction is vindicated.

Consider now, items a-d of section I:

**Item a: Spectrum spreading**

The present experiment typically showed a 10-13 db decrease in maximum $P_{IF}$ between the N=1 and N=3 cases. The frequencies involved preclude this fall-off being due to energy gap or capacitance effects (items b and d). The experiment was performed such that the junction properties remained essentially unchanged between the N=1 and N=3 cases for any given contact. The measured fall-off should therefore be a legitimate measure of the spreading of the supercurrent with increased N value. In the absence of a quantitative theory (based on the constant-current model) of $P_{IF}$ versus the several parameters discussed in this paper, the only further thing to be said is that the optimum "local oscillator" power in the N=1 case was from 6.5 to 11 dB less than that for the N=3 case.

**Item b: Energy gap**

For Nb, the binding energy (proportional to the energy gap) of an electron pair corresponds to a frequency of about 720 GHz. Since the highest drive frequency in this experiment was 25.1 GHz, energy gap effects should not have been a limitation. The laser experiments which are planned [21] will involve frequencies ~600 GHz to 4.25 THz (4250 GHz). Presumably the energy gap effect will then become important. Whether it will be possible to sort out the effects, a-d, one from another remains to be seen.

The present experiment does, however, have a potentially important bearing on this effect. The success in getting high quality junctions by plating Nb on W probably means that other superconducting materials would also work. Thus, for example, it may be possible to use Nb$_3$Sn or Nb$_3$Ge and essentially double the cutoff frequency due to this effect.

**Item c: Heating**

The analysis of Tinkham et al [10] on high frequency limitations due to heating, contains a parameter, $P_o$. This is essentially the level of ac power, absorbed by the junction, at which heating effects become important. They estimate the value of $P_o$ to be 10 µW. [This is based on adjusting the parameters of the theory to give a junction resistance (at large $V$) which is of the order of 10 ohms.] For the best contacts (17, 18, 21, 22), the local oscillator power at the top of the Josephson junction probe ranges from 36 µW (22) to 5 µW (18).

Since the characteristic impedance of the uniform part of the JJ probe is 50 ohms, the estimated values of absorbed power for #s 22 and 18 are 0.16 µW and 0.50 µW respectively. I would, therefore, tentatively conclude that heating was not a significant limitation in this experiment. Estimating the drive level necessary to maximize $P_{IF}$ for a laser frequency of 4.25 THz (N = 460), on the basis of the constant-voltage model [14], yields about 8 mW. It seems highly likely then, at the highest frequencies to which we intend to go, that heating will be a limitation.

**Item d: Capacitance**

Stewart has shown that when a junction is shunted by a sufficiently large capacitance, the resulting I-V curve will be hysteretic [21]. Others have realized this effect experimentally. A number of hysteretic I-V curves were obtained during the course of the present experiment. They are detrimental to obtaining good $P_{IF}$. Based on Stewart's work, an estimate has been made of the capacitance required to produce a hysteretic I-V curve typical of the present experiment. The result is 6.6 x
10^{-13} \text{ Farads}. If it is assumed that this capacity results from a dielectric barrier between the post and the tip of the whisker (assuming \( \varepsilon = 25 \varepsilon - \) the approximate dielectric constant of n-bium oxide – and a barrier thickness of \( 10^{-9} \text{ m} = 10 \text{ A}^*) \) then the cross sectional dimension of the effective parallel-plate capacitor would be 1.7 pm.

Microscopic examination of whiskers which have produced hysteretic I-V curves shows them to be blunted and with a flattened area whose cross sectional dimension is of the order of 2 pm. It is essential to note, however, that on several occasions, whiskers which have produced hysteretic I-V curves have been recontacted and the resulting I-V curve has not been hysteretic. In addition, junctions have been formed which never showed hysteresis and upon subsequent examination there was essentially no evidence of blunting. I tend to agree with Zimmerman that the usual contact dimension is usually significantly smaller than the radius of curvature of the tip [11]. Although the above calculation gives an upper limit to the capacitance, I know of no way to calculate a believable lower limit. As additional feeling for the numbers involved, if the cross sectional dimension were 0.5 pm then the capacitance would be \( 5.5 \times 10^{-14} \text{ Farads} \) and the resulting cutoff frequency would be about 0.6 THz.

An additional comment about high frequency limitations: The maximum IF obtained for the N=3 case was \( I = 3 \times 10^{-10} \text{ watts} \). If IF were proportional to \( N^2 \), then the output power at 4.25 THz would be about 1 \( \times 10^{-14} \text{ watts} \). Previous experience with essentially this same condition (extrapolated from N = 401 to N = 461) yielded about 2 \( \times 10^{-15} \text{ watts} \) [4]. There has been some experimental evidence for a fall-off in output going as \( N^{-2} \) and an analytical prediction of such behavior [4,7]. The data of Blyan et al. suggests, however, that the fall-off is more rapid if the laser frequency is above ~1 THz [9]. In sum: the spectrum spreading effect almost surely increases monotonically with increasing N value. For large N and large values of laser, it is likely that heating will be important; energy gap effects probably will be important, and a significant degradation due to contact capacitance cannot be ruled out.

V. CONCLUSIONS

At microwave frequencies, there are three characteristics which, if simultaneously present, appear to assure a PCJJ which is a good frequency multiplier and mixer. They are:

1. the critical current, \( I_c \), should be of the order of 250 \( \mu A \),
2. the undriven I-V curve should display "energy gap" structure,
3. the \( I_c R \) product should be of the order of 1 \( \mu V \) or greater.

The criterion of steps in the I-V curve, which is useful at laser frequencies, presents difficulties at microwave frequencies and this is discussed in the text.

The operational procedure – described in the appendix – of fabricating a PCJJ has a high probability of producing a good junction. In particular, the use of a tungsten whisker plated with a superconductor appears to be of significant importance in application.

There are four major effects that have potential for degrading multiplication and mixing performance at high frequencies. However, it is difficult to assess their absolute or even their relative effects at frequencies above about 1 THz. The present paper does, however, give quantitative information about spectrum spreading in going between the \( N=1 \) and \( N=3 \) cases at microwave frequencies.

ACKNOWLEDGEMENTS

Several people at NBS have been helpful in the work reported here. I am indebted to C.A. Hamilton for the use of his PCJJ mount and to L.O. Mullen for the fabrication of the Nb-plated tungsten whiskers. Discussions about Josephson junctions with J.E. Zimmerman were helpful. Useful comments on subject matter were made by R.M. Garvey, S.R. Stein and H. Hellwig.

APPENDIX

During the course of this work, a procedure has evolved which I have found to be very useful in producing a usable contact. In this procedure, one lead of an ordinary ohmeter (multimeter) is connected to the post and the other to the whisker. The ohmeter is set to the x10 scale and, if the contact is carefully made, the initial contact resistance - as indicated by the meter - is usually a few hundred ohms or more. The supercurrent at that time is almost always unacceptably small (less than 50 \( \mu A \)). The next step is not to further increase the pressure upon the contact (which will usually blunt the point) but rather to change the scale of the ohmeter to x10 and, perhaps, to x1.
x100 scale I try and get a junction to stabilize at about 200 ohms. A 200 ohm resistor draws 2.3 mA on this scale. Subsequent switching of a PCJJ down to the x10 scale usually results in a resistance of 20 - 30 ohms. A 26 ohm resistor draws 19 mA on this scale. Switching to x1 usually results in a 3-5 ohm resistance. A 4.4 ohm resistor draws 140 mA.) This often will result in a supercurrent of about the right magnitude.

If the $I_o$ is a little large or if the shape of the I-V curve needs improvement (in terms of the $I_o$ and energy gap criteria) then it is often possible to improve the junction by slightly backing off the pressure on the contact. Sometimes it is necessary to completely open the contact and begin the procedure again. In my experience this procedure has worked much more than half the time for the plated whiskers and the larger diameter whiskers. On the other hand, the often-used procedure of closing the contact with little or no bias across it has a high probability of damaging the tip beyond usefulness.

REFERENCES


FIGURE 1. The total dc current, \( I_t \), through the PCJ is plotted versus the dc voltage, \( V \), across it. For large values of \( V \) (say, \( V_1 \)) \( I_t \) asymptotically approaches the dashed line.

\[ R = V_1/I_1 \]

FIGURE 2. Block diagram of experimental set-up.

<table>
<thead>
<tr>
<th>EXTENT OF 2 ( I_0 ) (( \mu )A)</th>
<th>R ( I_o ) (ohms)</th>
<th>CONTACT ( P_{IF} ) # ( \mu )V ABOVE NOISE ( \mu )V ( \mu )V ABOVE NOISE</th>
<th>HYSTERETIC %</th>
<th>( I_o ) ( \mu )V FOR MAX ( P_{IF} ) (( \mu )V)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,000 580 N.M. (NOT MEASURED)</td>
<td>--</td>
<td>10</td>
<td>N.M.</td>
<td>Y</td>
</tr>
<tr>
<td>&gt; 700</td>
<td>680 2.8 0.95 16</td>
<td>41</td>
<td>30</td>
<td>*</td>
</tr>
<tr>
<td>&lt; 700 1,050</td>
<td>&lt; 1</td>
<td>--</td>
<td>3</td>
<td>N.M.</td>
</tr>
<tr>
<td>700</td>
<td>800</td>
<td>&lt; 1</td>
<td>--</td>
<td>11</td>
</tr>
<tr>
<td>700</td>
<td>1,500 &lt; 1</td>
<td>--</td>
<td>14</td>
<td>N.M.</td>
</tr>
<tr>
<td>600</td>
<td>1,400</td>
<td>&lt; 1</td>
<td>--</td>
<td>12</td>
</tr>
<tr>
<td>&gt; 500 180</td>
<td>&lt; 1</td>
<td>--</td>
<td>2</td>
<td>N.M.</td>
</tr>
<tr>
<td>450</td>
<td>530</td>
<td>&lt; 1</td>
<td>&lt; 0.5</td>
<td>20</td>
</tr>
<tr>
<td>420</td>
<td>1,600</td>
<td>&lt; 1</td>
<td>--</td>
<td>8</td>
</tr>
<tr>
<td>180</td>
<td>520</td>
<td>&lt; 1</td>
<td>--</td>
<td>7</td>
</tr>
<tr>
<td>NOT VISIBLE</td>
<td>480</td>
<td>&lt; 9</td>
<td>2.2</td>
<td>21</td>
</tr>
<tr>
<td>300</td>
<td>8.8</td>
<td>1.3</td>
<td>18</td>
<td>59</td>
</tr>
<tr>
<td>300</td>
<td>8.4</td>
<td>1.3</td>
<td>19</td>
<td>41</td>
</tr>
<tr>
<td>150</td>
<td>1.7</td>
<td>0.53</td>
<td>5</td>
<td>N.M.</td>
</tr>
<tr>
<td>560</td>
<td>6</td>
<td>1.17</td>
<td>22</td>
<td>53</td>
</tr>
<tr>
<td>200</td>
<td>4.5</td>
<td>0.45</td>
<td>1</td>
<td>20</td>
</tr>
<tr>
<td>400</td>
<td>4.2</td>
<td>0.94</td>
<td>17</td>
<td>57</td>
</tr>
<tr>
<td>320</td>
<td>4.0</td>
<td>0.94</td>
<td>24</td>
<td>47</td>
</tr>
<tr>
<td>140</td>
<td>2.0</td>
<td>0.14</td>
<td>4</td>
<td>N.M.</td>
</tr>
<tr>
<td>50</td>
<td>0.9</td>
<td>0.045</td>
<td>6</td>
<td>25</td>
</tr>
<tr>
<td>1,800</td>
<td>&lt; 1</td>
<td>--</td>
<td>15</td>
<td>51</td>
</tr>
</tbody>
</table>

\( + = 0.002'' \) SOLID Nb  \( \dagger = 0.005'' \) SOLID Nb  \( * = 0.002'' \) Nb-PLATED W