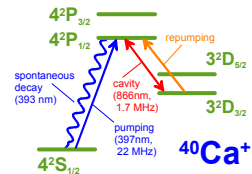


Introduction

A single Ca-ion, trapped in an r.f. quadrupole trap and placed between mirrors of a high finesse optical cavity, is an ideal system to deterministically control the interaction between an atom and a single mode of the radiation field. By confining the ion to a region smaller than its transition wavelength, a well-defined and stationary atom-field coupling strength is achieved. This system can be employed to generate single photons on demand, to map the quantum state between the ion and a photon and to entangle the ion and a photon. Two ions coupled to optical cavities have been proposed for quantum state transfer and entanglement of ions.



Using a high-finesse cavity on the 866 nm transition of the ⁴⁰Ca⁺ level-scheme provides ideal conditions for reaching the strong-coupling regime of cavity QED with a single ion.

Setup: linear Paul trap and cavity

Trap design:

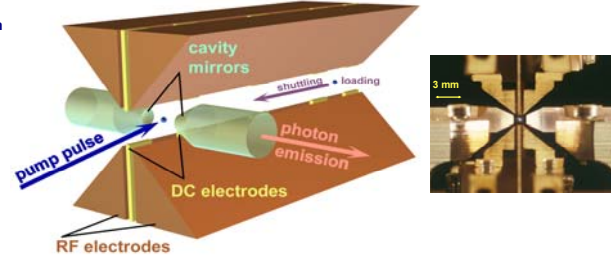
Linear r.f. trap with open electrode configuration

- trap frequency $\Omega = 2\pi \times 12.7$ MHz
- radial confinement $\omega_r = 2\pi \times 1.1$ MHz
- axial confinement $\omega_z = 2\pi \times 0.3$ MHz

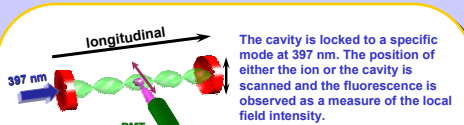
Cavity design:

Fabry-Perot cavity with adjustable length

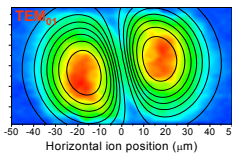
- length: $L = 0.8 \dots 10$ mm
- waist: $W_0 = 23 \dots 37$ μ m
- damping: $\kappa/2\pi = 1.0 \dots 0.2$ MHz
- coupling: $g/2\pi = 4.6 \dots 0.8$ MHz



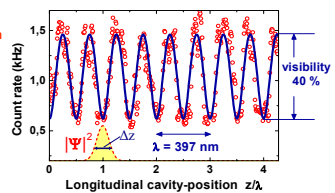
Single-ion mode mapping



Two-dimensional images of cavity modes obtained by scanning the ion horizontally and the cavity position vertically.



Longitudinal scan of cavity modes obtained by scanning the cavity along its axis with respect to the ion's position.

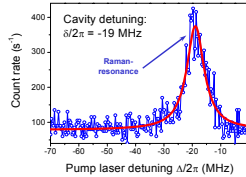
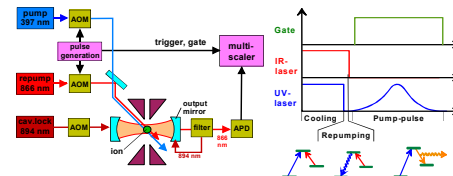


Visibility reduced by the spread of the ion's wave function Δz :

$$\Delta z = 42 \text{ nm} \rightarrow 2\% \text{ variation of } g \text{ (} \lambda/10 \text{)} \rightarrow \text{Deterministic ion-field coupling}$$

Single-photon gun

Continuous generation of single photon pulses by applying a sequence of cooling, repumping and pump pulses to a single ion



Single photon peak observed by scanning the frequency of the pump laser.

Efficiency: 8%

Applications of a deterministic single-photon source:

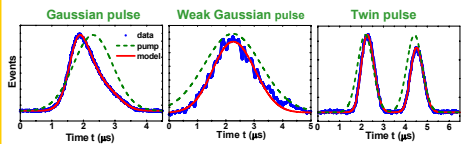
- quantum cryptography
- quantum communication
- quantum computation

J. McKeever, A. Boca, A. D. Boozer, R. Miller, J. R. Buck, A. Kuzmich, H. J. Kimble, Science 303, 1992 (04)
M. Hennrich, T. Legero, A. Kuhn, G. Rempe, PRL 85, 4872 (00)
J. Kim, O. Benson, H. Kan, Y. Yamamoto, Nature 397, 500 (99)
C. K. Law, H. J. Kimble, J. Mod. Opt. 44, 2067 (97)

Single-photon emission

Single-photon pulseshapes

Statistics of single photon detection times with respect to trigger (pump) \rightarrow Temporal structure of single photon pulse

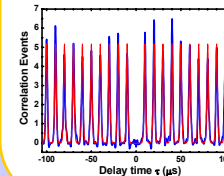


Arbitrary control over temporal structure of single photon pulse

- Limitations: - effective Rabi frequency
- cavity decay

Second-order correlations

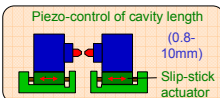
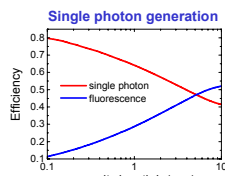
Measure cross-correlations \rightarrow $g^{(2)}$ -function



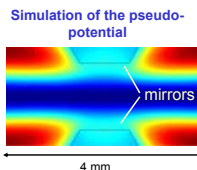
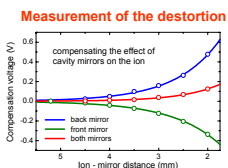
$g^{(2)}(0) = 0$
 \updownarrow
single photon
 $\frac{P_1^2}{2P_2} > 68$
68 times better suppression of two photon events compared to a poissonian source

Influence of mirrors on trap potential

Increase efficiency and fidelity of quantum operations by decreasing the cavity length



Measuring the influence of the mirrors on the trapping potential by observing the compensation voltage of the micrometer for different cavity lengths.



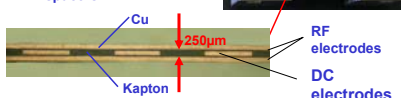
Strong influence of the mirrors on the trapping potential even for long cavities

Stable trapping conditions: Cavity length > 4mm

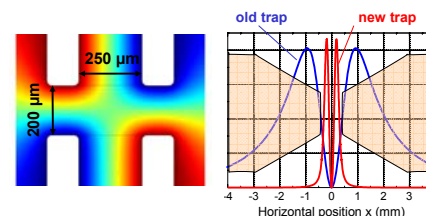
New trap design

Small cavity which does not perturb the trapping field requires small trap structure

made from 125 μ m copper sheet, glued together with Kapton spacers



Radial RF field distribution: Pseudo-potential (horizontal):



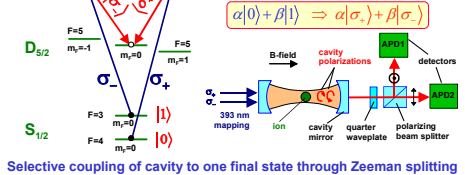
Less overlap of field and mirrors \rightarrow 0.5mm cavity length feasible

Ion-photon coupling

Mapping of quantum information

Make single photon emission dependent on quantum state

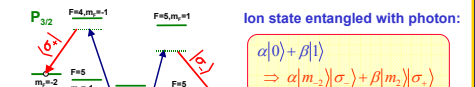
Ion state mapped to photons with different circular polarizations:



Selective coupling of cavity to one final state through Zeeman splitting

Ion-photon entanglement

Choose different final states for ion:



Ion state entangled with photon:
 $\alpha|0\rangle + \beta|1\rangle \Rightarrow \alpha|m_{-1}\rangle|\sigma_{-}\rangle + \beta|m_{+1}\rangle|\sigma_{+}\rangle$

Application: Entanglement of ions in distant traps (entanglement distribution)